

## Subject: Mathematics

### MATH-H-GE-T-04 (Calculus & Differential Equations)

Full Marks:10

Answer all the questions.

$2 \times 5 = 10$

1. If  $y = \sin(m \sin^{-1} x)$ , then show that

$$(1 - x^2)y_{n+2} - (2n + 1)xy_{n+1} + (m^2 - n^2)y_n = 0$$

2. Find the maximum value of  $x^{\frac{1}{x}}$ ,  $x > 0$ .

Submit answer script to the mail id: [mathematics@nvc.ac.in](mailto:mathematics@nvc.ac.in)

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### MATH-G-CC-T-04 (Linear Programming Problems & Game Theory)

Full Marks: 10

Answer all the questions.

$2 \times 5 = 10$

1. Solve graphically the L.P.P

$$\text{Maximize } z = 4x_1 + 7x_2$$

Subject to,

$$2x_1 + 5x_2 \leq 40$$

$$x_1 + x_2 \leq 11$$

$$x_2 \geq 4$$

$$x_1 \geq 0, x_2 \geq 0$$

2. Find the optimal solution of the following transportation problem

	D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>	D <sub>4</sub>	
O <sub>1</sub>	9	8	5	7	12
O <sub>2</sub>	4	6	8	7	14
O <sub>3</sub>	5	8	9	5	16
	8	18	13	3	

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### MATH-G-SEC-T-2A (Graph Theory)

Full Marks:10

Answer all the questions.

$2 \times 5 = 10$

1. Let  $G$  be a simple graph. Prove that if  $G$  is not connected then its complement  $\bar{G}$  is connected.

2. Prove that, A simple graph is connected if and only if it has a spanning tree.

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