

ASSIGNMENT-1

Answer all questions.

$5 \times 4 = 20$

1. Find the order of the permutation

$$\begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 \\ 4 & 6 & 3 & 5 & 1 & 2 \end{pmatrix}$$

2. Show that the order of a permutation on a finite set is the l.c.m. of the lengths of the disjoint cycles.

3. Let $s = \{1,2,3,4\}$ and

$$f = \begin{pmatrix} 1 & 2 & 3 & 4 \\ 1 & 3 & 4 & 2 \end{pmatrix}, g = \begin{pmatrix} 1 & 2 & 3 & 4 \\ 2 & 3 & 4 & 1 \end{pmatrix}, h = \begin{pmatrix} 1 & 2 & 3 & 4 \\ 1 & 3 & 4 & 2 \end{pmatrix}$$

Then show that $f(gh) = (fg)h$

4. Examine whether the composition \circ on $M_2(R)$ defined by

$$A \circ B = \frac{1}{2}(AB - BA), A, B \in M_2(R)$$

is (i) commutative, (ii) associative.

5. Write the composition table for the binary operation multiplication modulo 10 (\times_{10}) on the set $\{2,4,6,8\}$ and hence check the operation is commutative or not.