

Internal Examination 2020
DEPARTMENT OF MATHEMATICS
3rd SEMESTER

MATH-H-CC-T-05

Theory of Real Functions & Introduction to Metric Space

1. Using $\varepsilon - \delta$ definition verify $\lim_{x \rightarrow 3} \frac{1}{x} = \frac{1}{3}$ 3
2. Using sequential criterion show that $\lim_{x \rightarrow 0} \cos \frac{1}{x}$ does not exist. 3
3. Let f be defined on \mathbb{R} by
$$f(x) = \begin{cases} 1, & \text{if } x \text{ is rational} \\ 0, & \text{if } x \text{ is irrational} \end{cases}$$
Show that f is not continuous at any point of \mathbb{R} . 4

MATH-H-CC-T-06

Group Theory 1

1. If G be a group and H be a non-empty subset of G then prove that H is a subgroup of G if for each $x, y \in H, xy^{-1} \in H$. 5
2. Which one of the following is a group and why?:
 $\langle \mathbb{N}, + \rangle, \langle \mathbb{N}, - \rangle$ 5

MATH-H-CC-T-07

Numerical Methods & Numerical Methods Lab

1. Discuss advantage and disadvantage of Newton Forward Interpolation formulae.
2. Deduce Lagrange's interpolation formulae.

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MATH-H-SEC-T-1A

Logic and Sets

1. For any three sets A,B,C prove that

$$A \Delta (B \Delta C) = (A \Delta B) \Delta C$$

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2. Show that the relation defined on \mathbb{Z} by

$$\rho = \{(x, y): 3x + 4y \text{ is divisible by } 7\}$$

is an equivalence relation.

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